6-1 Slope of a Line and Slope-intercept Form

Standards

- B.S.ID.C.4 Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data
- B.F.IF.C.4 Graph linear, quadratic, absolute value, and piecewise functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated ones.
- B.N.Q.A.1 Use units as a way to understand problems and to guide the solution of multistep problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.

Objective

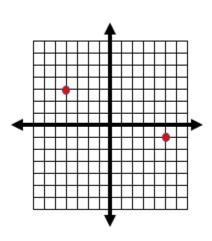
- SWBAT use linear equations IOT solve problems in context .
- SWBAT write the slope-intercept form of an equation IOT graph the equation.

Key Concepts

<u> </u>	the steepness, or rise over run, or rate of change given by the
formula $m = \frac{y_2 - y_1}{x_2 - x_1}$	
	the point in which the graph crosses the <i>x</i> -axis.
	the point in which the graph crosses the <i>y</i> -axis.
	y = mx + b, where $m =$ slope and $(0, b)$ is the y-intercept.

Examples

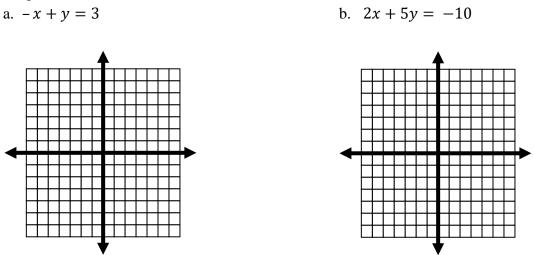
- 1. Find the slope of AB containing the points A(-1, 2) and B(3, -4).
- 2. Find the slope of XY.
- 3. Graph the line that passes through G(1, 1) and has a slope of $-\frac{3}{4}$.



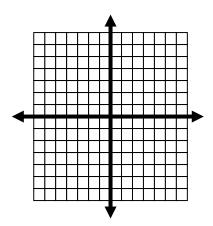
4. Find the slope and *y*- intercept.

a.
$$y = \frac{2}{3}x - 4$$
 b. $2x + 3y = 6$

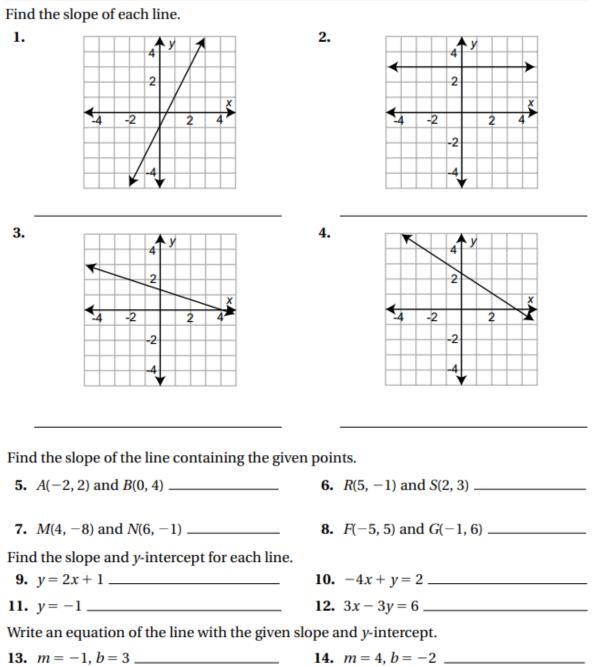
- 5. Write the equation for the line with the given slope and *y*-intercept.
 - a. m = 2, b = -4 b. m = 0, b = 1 c. $m = \frac{3}{4}, b = 0$
- 6. Graph the line



7. Production figures for an assembly plant are represented by a line with a slope of $\frac{1}{2}$ and a *y*-intercept of -1. Find the equation of the line. Then draw the graph of the line.







6-3 Write Equations for Lines

Standards

- B.S.ID.C.4 Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.
- B.A.CED.A.3 Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.

Objective

• SWBAT write equations for lines in point-slope form IOT solve problems in context.

Key Concepts

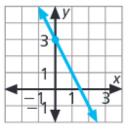
- $y - y_1 = m(x - x_1)$ where m = slope and (x_1, y_1) is a point on the line.

Ax + By = C where A, B and C are integer coefficients.

lf you know	You can write an equation in	
1. The slope <i>m</i> and <i>y</i> -intercept <i>b</i> 2. A point $(x_1 y_1)$ and the slope <i>m</i> 3. Two points $(x_1 y_1)$ and $(x_2 y_2)$	1. Slope-intercept form: $y = mx + b$ 2. Point slope form: $y - y_1 = m(x - x_1)$ 3. Point slope form: $y - y_1 = m(x - x_1)$ or $y - y_2 = m(x - x_2)$ where $m = \frac{y_2 - y_1}{x_2 - x_1}$	
4. The graph with points $A(x_1 y_1)$ and $B(x_2 y_2)$	4. Same as 3.	

Examples

- 1. Write an equation of the line with a slope of -2 and passes through the point P(-1, 3).
- 2. Write an equation of the line through A(1, -3) and B(3, 2).
- 3. Write the equation of the line shown.



- 4. Write the equation $y = -\frac{1}{2}x + 1$ in standard form.
- 5. Write the equation of the line parallel to $y = -\frac{1}{3}x + 1$ containing R(1, 1).
- 6. Write the equation of the line perpendicular to $y = -\frac{1}{3}x + 1$ containing R(1, 1).
- 7. The temperature of water at the freezing point is 0°C or 32°F. The temperature of water at the boiling point is 100°C or 212°F. Use these two data points to find an equation to convert the temperature from Celsius to Fahrenheit.

-----Lesson 6-3 Independent Practice/Lesson Check------

Write an equation of the line with the given slo	ope and y-intercept.
1. $m = -2, b = 4$	2. $m = -\frac{2}{5}, b = 1$
3. $m = -5, b = -2$	4. $m = 1, b = \frac{3}{4}$
Write an equation of the line with the given in $5 - 3 - 6 - 6 = 0$	6. $m = \frac{1}{3}, W(\frac{1}{2}, 2)$
5. $m = 0, C(-1, 4)$	6. $m = \frac{1}{3}, W(\frac{1}{2}, 2)$
7. <i>m</i> is undefined, <i>T</i> (5, −6)	8. $m = -4, S\left(\frac{3}{5}, -\frac{1}{5}\right)$
9. <i>A</i> (3, -1) and <i>B</i> (2, 4)	10. <i>M</i> (-6, 4) and <i>N</i> (0, -5)
11. <i>R</i> (6, -1) and <i>S</i> (-3, 0)	12. <i>F</i> (1, -8) and <i>G</i> (3, 2)
13. $\begin{array}{c ccccccccccccccccccccccccccccccccccc$	

15. Parallel to x + y = 4 and passes through M(3, 2).

Name:	Date:	Period:

6-4 Systems of Equations

Standards

- B.A.REI.C.3 Solve and explain the solutions to a system of equations using a variety of representations including combinations of linear and non-linear equations.
- B.A.CED.A.2 Create equations in two or more variables to represent relationships between quantities.

Objective

- SWBAT use graphical means IOT solve a linear system of equations.
- SWBAT analyze a system IOT determine the number of solutions.

Key Concepts

_____- two linear equations with the same two variables

_____- the point of intersection of the lines in the system.

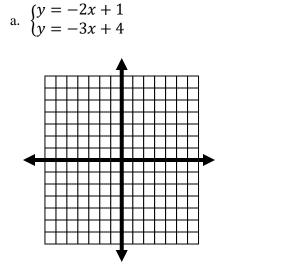
_____- systems that have lines intersecting at one point.

_____- systems in which the lines coincide and every point on the line is a solution. This system has infinitely many solutions.

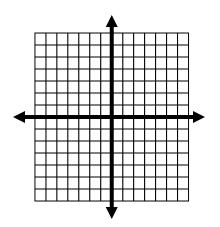
_____- systems that have lines that do not intersect.

Examples

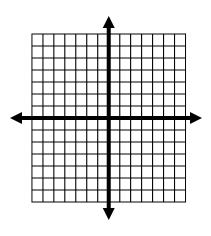
1. (I do) Solve the system by graphing.



b.
$$\begin{cases} y = \frac{1}{2}x + 3\\ 2y = x - 2 \end{cases}$$



2. (We do) Use technology to graph. $\begin{cases} 4x + 2y = 8\\ 6x + 3y = 12 \end{cases}$

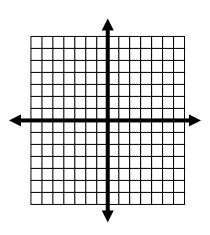


3. (We do) Determine whether (2, 1) is a solution of the system $\begin{cases} 5y = 3x - 1\\ 2x - 3y = 1 \end{cases}$

4. (We do) Determine the number of solutions for the system. Do not graph.

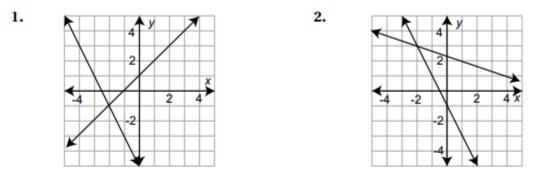
(4x + 5y = 3)	(x + y = 3)	(4x + 5y = 3)
a. $\begin{cases} 4x + 5y = 3\\ 3x - 2y = 8 \end{cases}$	b. $\begin{cases} x+y=3\\ 2x+2y=6 \end{cases}$	c. $\left\{ y = -\frac{4}{5}x - 1 \right\}$

5. (They Do) The sum of 2 numbers is -3. Their difference is 13. Find the numbers by writing a system of equations and solving by graphing.

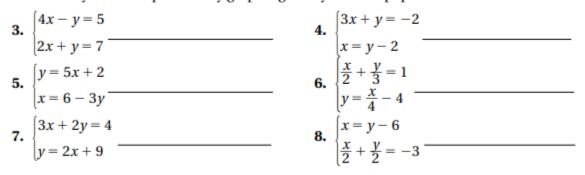


-----Lesson 6-4 Independent Practice/Lesson Check------

Determine the solution of each system of equations.



Solve each system of equations by graphing. Use your own paper.



- 9. The sum of two numbers is 2. Their difference is 10. Find the numbers.
- One number is three times another number. The difference of the two numbers is
 Find the numbers.

Name:	Date:	Period:

6-5 Solving Systems of Equations by Substitution

Standards

- B.A.REI.C.3 Solve and explain the solutions to a system of equations using a variety of representations including combinations of linear and non-linear equations.
- B.A.CED.A.2 Create equations in two or more variables to represent relationships between quantities.

Objective

• SWBAT use substitution IOT solve a linear system of equations.

Key Concepts

- If a = b, a may replace b in any mathematical expression. This method can be used to solve systems of equations.

Examples

1. (I do) Solve the system using substitution.

a.
$$\begin{cases} 3x - y = 6 \\ x = -2y + 2 \end{cases}$$
 b.
$$\begin{cases} x + 3y = -9 \\ -5x - 2y = -7 \end{cases}$$

2. (We do) Solve the system using substitution.

a.
$$\begin{cases} 2x + 3y = 6\\ 4x + 6y = 6 \end{cases}$$
 b.
$$\begin{cases} 4x - 2y = 10\\ -2x + y = -5 \end{cases}$$

3. (They do) An appliance store delivers large appliances using vans and trucks. When loaded, each van holds 4 appliances and each truck holds 6 appliances. If 42 appliances are delivered by 8 full vehicles, how many vans and trucks are used?

-----Lesson 6-5 Independent Practice/Lesson Check------

Solve each system of equations by the substitution method. Check the solution.

1. $\int x + y = 4$	2. $\int 5x + y = 0$
2x - y = 5	x - 2y = 11
3.	4. $\begin{bmatrix} 2x + \frac{1}{2}y = 25 \\ -x - y = 10 \end{bmatrix}$

- 15. Ryan has 10 coins consisting of dimes and nickels worth \$0.70. How many dimes and how many nickels does he have? ______
- 16. Brooke spent \$94.92 at the music store. She bought some cassette tapes for \$9.99 each and some CDs for \$12.99 each. How many cassette tapes and how many CDs did she buy if she bought 8 all together?

Name:	Date:	Period:

6-6 Solving Systems of Equations by Elimination (Adding & Multiplying)

Standards

- B.A.REI.C.3 Solve and explain the solutions to a system of equations using a variety of representations including combinations of linear and non-linear equations.
- B.A.CED.A.2 Create equations in two or more variables to represent relationships between quantities.

Objective

• SWBAT use elimination IOT solve a linear system of equations.

Key Concepts

- using the Addition Property of Equality or using additive inverses to cancel a variable.

Examples

1. (I do) Solve the system using elimination.

a.
$$\begin{cases} x - y = -5 \\ x + y = 1 \end{cases}$$
 b.
$$\begin{cases} 2x + 7y = -5 \\ -5x + 7y = -12 \end{cases}$$

2. (We do) Solve the system using elimination.

a.
$$\begin{cases} 3x - 4y = 10 \\ 3y = 2x - 7 \end{cases}$$
 b.
$$\begin{cases} 3x - 5y = -1 \\ 6x = -2y + 10 \end{cases}$$

3. (They do) Rodrick sold 25 movie tickets for a total of \$132. If each adult ticket sold for \$6 and each children's ticket sold for \$4. How many of each kind did he sell?

------Lesson 6-6 Independent Practice/Lesson Check------

Exercises

Solve each system of equations. Check the solu	Solve each system of equations. Check the solution.			
$ \begin{array}{c} 1. & 2x - y = 4 \\ x + 2y = 7 \end{array} $	2. $\begin{bmatrix} 3x - y = 4 \\ 4y = -2x + 12 \end{bmatrix}$			
3. $\begin{cases} x = 3y - 6 \\ 6y = x + 3 \end{cases}$	$\begin{array}{c} 4. \begin{bmatrix} -x+3y=8\\ y=2x-4 \end{bmatrix}$			
5. $\begin{cases} 6x + 6y = 6 \\ x + y = 1 \end{cases}$	6. $\begin{bmatrix} 5x - y = 4 \\ 3x = -2y + 18 \end{bmatrix}$			
7. $\begin{cases} 3y = 2x - 9 \\ 6x + 13 = y \end{bmatrix}$	8. $\begin{cases} 10x + 5y = 20 \\ x = y + 2 \end{cases}$			

9. The perimeter of a rectangle is 24 in. The length is twice the width. Find the dimensions.

Name:	Date:	Period:	

6-7 Solving Systems of Equations using Matrices

Standards

- B.A.REI.C.3 Solve and explain the solutions to a system of equations using a variety of representations including combinations of linear and non-linear equations.
- B.A.CED.A.2 Create equations in two or more variables to represent relationships between quantities.

Objective

• SWBAT use matrices IOT solve a linear system of equations.

Key Concepts

_____- a rectangular array of elements.

Examples

1. (I do) Solve the system using matrices.

a.
$$\begin{cases} 2x - y = 4 \\ -3x + 2y = 5 \end{cases}$$
 b.
$$\begin{cases} x + 3y = 4 \\ -2x + y = -1 \end{cases}$$

2. (We do) Solve the system using a matrix $\begin{cases} 3x - y = 2\\ 2y = -x - 4 \end{cases}$

3. (They do) Enterprise Rental charges \$25 per day plus \$0.35 per mile. Avis charges \$35 per day plus \$0.25 per mile. Carter determines the trip he needs to take will cost \$230 with Enterprise and \$250 with Avis. How many miles and for how many days will Carter's trip be?

-----Lesson 6-7 Independent Practice/Lesson Check-----

For each system of equations, **a.** write the matrix equation and **b.** solve using the method of determinants.

1.	-3x + 4y = 12 $x - 2y = 6$	a	b
2.	5x + y = 10 $x - y = 5$	a	b
3.	$\begin{cases} x - y = 16\\ x + y = 10 \end{cases}$	a	b
4.	2x - 2y = 8 $-x + 3y = 12$	a	b

6-8 Linear Systems of Inequalities

Standards

- B.A.CED.A.1 Create equations and inequalities in one variable and use them to solve real world problems.
- B.A.REI.C.3 Solve and explain the solutions to a system of equations using a variety of representations including combinations of linear and non-linear equations.
- B.A.REI.D.5 Solve a linear inequality using multiple methods and interpret the solution as it applies to the context.

Objective

- SWBAT model a real-world situation using systems of linear inequalities.
- SWBAT use graphs to solve a system of linear inequalities.

Key Concepts

_____- two or more inequalities with the same variables.

_____- the intersection of the graphs of the inequalities.

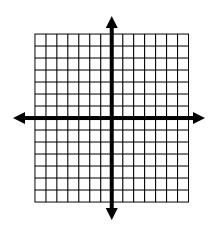
Examples

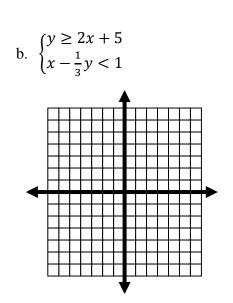
1. (I do) Determine whether the given ordered pair is a solution to the given system of inequalities.

a. (2, -5);
$$\begin{cases} 4x - y \ge 5\\ 8x + 5y \le 3 \end{cases}$$
 b. (1, 2);
$$\begin{cases} x + y \ge 3\\ 3x - y < 1 \end{cases}$$

2. (We do) Graph the solution set to the system.

a.
$$\begin{cases} 2x - 3y \le 6\\ x + 2y < 2 \end{cases}$$

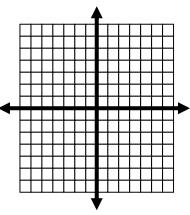




3. (We do) Write a system of inequalities for the graph.

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		4	Ħ	Ħ	Ħ
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4			Y		
	4 -2	2	1		
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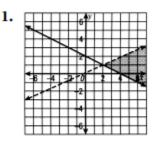
4. (They do) Jasmine needs to earn at least \$100 this week. She earns \$6 per hour doing gardening and \$8 per hour as a part-time receptionist. She has only 18 h available to work during the week. Write and graph a system of linear inequalities that models the weekly number of hours Jasmine can work at each job and how much money she needs to earn.

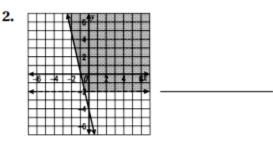




Exercises

Write a system of linear inequalities for each graph.





Graph the solution set of each system of linear inequalities on another sheet of paper.

3. $\begin{cases} x > 2 \\ y > 4 \end{cases}$ **4.** $\begin{cases} x < y + 1 \\ 3 \le -x - y \end{cases}$ **5.** $\begin{cases} x + y \ge 0 \\ y - x < 4 \end{cases}$